On a Sufficient Condition for the Existence of Stein Neighborhood Bases

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Abstract

This is a report on work in progress. Sibony showed that if a smooth bounded pseudoconvex domain Ω in \mathbb{C}^n satisfies McNeal's property (\tilde{P}) (or Catlin's property (P)), then $\overline{\Omega}$ has a Stein neighborhood basis. In this talk, we give a sufficient condition that is weaker than property (\tilde{P}) but still implies the existence of a Stein neighborhood basis for the closure. We will give some applications to domains in \mathbb{C}^n that have plurisubharmonic defining functions and to domains in \mathbb{C}^2 with a defining function that is pluriharmonic on weakly pseudoconvex points.