Growth Tight Actions

Christopher Cashen

Abstract: (Joint with Arzhantseva, Tao) We study the growth rate of an orbit of a group G acting on a geodesic metric space X. We impose geometric conditions that control the distortion of the orbit and guarantee that G acts in a direction that looks hyperbolic, and conclude that the growth rate of the orbit of G is strictly larger than the growth rate of its quotients. Examples of such actions include groups acting geometrically on hyperbolic spaces, relatively hyperbolic spaces, and many CAT(0) spaces. Examples also include the action of the mapping class group of a hyperbolic surface on its Teichmueller space.