# ON A PROBLEM ABOUT COVERING LINES BY SQUARES 

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Abstract. - Let $S$ be the square $[0, n]^{2}$ of side length $n \in \mathbb{N}$ and let $\mathcal{S}=\left\{S_{1}, \ldots, S_{t}\right\}$ be a set of unit squares lying inside $S$, whose sides are parallel to those of $S$. The set $\mathcal{S}$ is called a line cover, if every line intersecting $S$ also intersetcs some $S_{i} \in \mathcal{S}$. Let $\tau(n)$ denote the minimum cardinality of a line cover, and let $\tau^{\prime}(n)$ be defined in the same way, except that we restrict our attention to lines which are parallel to either one of the axes or one of the diagonals of $S$. It has been conjectured by L.F. Tóth that $\tau(n)=2 n+0(1)$ and I. BÁrányi and Z. Füredi that $\tau(n)=\frac{3}{2} n+0(1)$. We will prove instead, $\tau^{\prime}(n)=\frac{4}{3}+0(1)$, and as to TóTh's conjecture, we will exhibit a "non integer" solution to a related LP-relaxation, which has size equal to $\frac{3}{2}+0(1)$.

## REFERENCES

[T] Fejes Tóth (L.). - Remarks on a dual of Tarski's plank problem, Mat. Lapok, t. 25, 1974, p. 13-20.
[M] Moser (W.O.) and Pach (J.). - Research Problems in Discrete Geometry, Problem 84, Montréal, 1984, mimeographed.
[BF] BÁrÁNyi (L.) and Füredi (Z.). - Covering all secants of a square, Rutcor Research Report 3-36, Rutgers Univ., New Brunswick, N.J., March 1986.

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