Wave-particle and wave-wave interactions in the Solar Wind: simulations and observations

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"Ion kinetics in the solar wind: coupling global expansion to local microphysics" in press at Space Sci. Rev.

Outline

- Adiabatic expansion of a plasma
- Role of Coulomb collisions
- Wave-particle interactions: instabilities and plasma heating
- Wave-wave interactions: Non-linear evolution of Alfvén waves
- Evolution at oblique propagation

Why wave-particle interactions?

- In collisionless plasmas, collisions between particles are not able to maintain the equilibrium (Maxwellian distributions).
 Wave-particle interactions control the plasma thermodynamics.
- Particle distribution far for equilibrium can excite instabilities and generate fluctuations.
- Wave-wave interactions (3-w couplings, turbulence) can also produce fluctuations that involve particle dynamics.

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Interesting for many astrophysical plasmas

The solar wind



• High latitudes

Fast wind: 750 km/s and density of 3 particles/cm³ at 1AU; regular.

• Equatorial regions

Slow wind: bulk speed 350 km/s 10 particles/cm³ at 1 AU; irregular.

Particle distribution functions are not Maxwellian, far from the LTE!

magnetic field

Helios observations in the solar wind



 Temperature anisotropy between parallel and perpendicular directions with respect to the ambient

$$T_{\perp} \neq T_{\parallel}$$

Velocity beam in the parallel direction

(Marsch et al. 1982)

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Interactions in a plasma - Schematic view



(e.g., Alexandrova 2010, Araneda 2008&2009, Bourouaine 2010&2011, Califano 2008, Kunz 2011, Henri 2008, Passot&Sulem 2003&2006, Schekochihin 2009&2010, Valentini 2008&2009...)

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... but spherical expansion!





V⊥

$$\mu = v_{\perp}^2/B$$
 $v_{\perp} \propto r^{-1}$
 $E_{hin} = v_{\perp}^2 + v_{\perp}^2$



V⊥

$$\mu = v_\perp{}^2/B$$
 $v_\perp \propto r^{-1}$ $E_{kin} = v_\parallel^2 + v_\perp^2$

 v_{\parallel}



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Evolution of solar wind proton distribution functions



Evolution of solar wind proton distribution functions



CGL or Double Adiabatic

$$\frac{\mathrm{d}}{\mathrm{dt}} \left(\frac{P_{\perp}}{nB} \right) = 0 \quad \text{and} \quad \frac{\mathrm{d}}{\mathrm{dt}} \left(\frac{P_{\parallel}B^2}{n^3} \right) = 0$$
$$T_{\perp p} \propto B \quad \text{and} \quad T_{\parallel p} \propto \frac{n^2}{B^2} ;$$
$$\left(\frac{\mathrm{d}v_{\mathrm{s}\parallel}}{\mathrm{d}t} \right)_{\mathrm{CGL}} = \frac{v_{\mathrm{s}\parallel}}{n} \frac{\mathrm{d}n}{\mathrm{d}t} - \frac{v_{\mathrm{s}\parallel}}{B} \frac{\mathrm{d}B}{\mathrm{d}t}$$

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Expansion in a radial magnetic field

$$T_{
m p\perp} \propto R^{-2} ~~{
m and}~~T_{
m p\parallel} = {
m const}$$
 $v_{
m s\parallel} = {
m const}$

only if
$$T_{\parallel} = T_{\perp} = T$$
 then $T \propto R^{-4/3}$

The observed evolution of protons between 0.3 and 1 AU



Helios observations

$$eta_{\mathrm{p}\parallel} \propto rac{nT_{\mathrm{p}\parallel}}{B^2} \propto R^2 \propto T_{\mathrm{p}\parallel}/T_{\mathrm{p}\perp}$$

Non-adiabatic, presence of perpendicular heating
Change of slope observed at 1 AU (β>1)

Estimated number of collisions at 1 AU

Protons

$$N = \frac{\tau_{exp}}{\tau^p_{coll}} = \frac{L}{\lambda} \frac{v^p_{th}}{v_{sw}} = K_n^{-1} \frac{v^p_{th}}{v_{sw}} < 1$$

Electrons

$$N = \frac{\tau_{exp}}{\tau^e_{coll}} = \frac{L}{\lambda} \frac{v^e_{th}}{v_{sw}} = K_n^{-1} \frac{v^e_{th}}{v_{sw}} > 1$$

WIND observations (after *Kasper et al. PRL 2008, Bale et al. PRL 2009*)



See also Bourouaine's presentation and *Bourouaine et al. ApJ 2011*

Evolution of a plasma with an alpha-proton drift (adiabatic vs. weakly collisional)



Evolution of a plasma with an alpha-proton drift (adiabatic vs. weakly collisional)



The decrease of the velocity drift by collisions tends to increase the alpha to proton temperature ratio!

Evolution of a plasma with an alpha-proton drift (Hybrid numerical simulations)





Matteini et al., GRL 2007

$$\beta_{\parallel,\perp} = \frac{P_{\parallel,\perp}}{B_0/8\pi} = \frac{8\pi n k_B T_{\parallel,\perp}}{B_0^2}$$



Linear theory with a 5% of alpha particles

Matteini et al., GRL 2007

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Linear theory with a 5% of alpha particles



Linear theory with a 5% of alpha particles





Non-adiabatic evolution, local perpendicular heating.



Non-adiabatic evolution, local perpendicular heating.



Non-adiabatic evolution, local perpendicular heating.

Local generation of fluctuations. Enhancement of wave activity observed by WIND (*Bale et al. 2009*) and Ulysses (Wicks et al. 2010)



Slow wind: WIND data (Kasper et al. 2002, Hellinger et al. 2006, Matteini et al. 2011)



Parallel fire hose

Oblique fire hose





$$T_{\parallel} \simeq 2.7 \cdot 10^{5} (R/R_{0})^{-0.54} \text{ K},$$

$$T_{\perp} \simeq 2.4 \cdot 10^{5} (R/R_{0})^{-0.83} \text{ K},$$

$$T \simeq 2.5 \cdot 10^{5} (R/R_{0})^{-0.74} \text{ K},$$

$$q_{\parallel} \simeq 4.8 \cdot 10^{-7} (R/R_{0})^{-2.9} \text{ W/m}^{2},$$

$$q_{\perp} \simeq 4.8 \cdot 10^{-8} (R/R_{0})^{-2.8} \text{ nW/m}^{2},$$

$$q \simeq 2.0 \cdot 10^{-7} (R/R_{0})^{-2.8} \text{ W/m}^{2}.$$



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$$Q_{\perp} = nk_{\rm B}(\boldsymbol{u}\cdot\boldsymbol{\nabla}T_{\perp}+T_{\perp}\boldsymbol{\nabla}_{\perp}\cdot\boldsymbol{u}),$$





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Alfvén waves in space plasmas



B-v correlation, |B| and n almost constant, E(z+)>E(z-)

Wave-wave coupling: Parametric instability Field and spectrum signatures



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Wave-wave coupling: Parametric instability and beam generation (see also Araneda's talk et *Araneda 2008*)

Proton phase space x-vx



Parametric decay of a monochromatic Alfvén wave (Matteini et al. JGR 2010)

Wave-wave coupling: Parametric instability and beam generation (see also Araneda's talk et *Araneda 2008*)



Beam properties with different betas

The Hybrid Expanding Box code (HEB)

To study non-linear wave-particle interactions during the solar wind expansion, we perform numerical simulation using a hybrid code implemented with an expanding box model

(Liewer et al. 2001, Hellinger et al. 2003).

- Hybrid model: electrons are described as an isotropic massless fluid and protons (ions) as particles (*Matthews 1994*).
- The expanding box model assumes a radial linearly driven evolution with a constant expansion velocity; the transverse dimensions of the box (which co-moves with the wind) increase with distance (*Grappin et al. 1993*).



Adiabatic evolution for ions (CGL) and waves (WKB)

Self-consistent competition between the cooling driven by the expansion and the heating provided by wave-particle interactions and wave-wave instabilities

Evolution of a spectrum of outward Alfvén waves Expanding simulation



Wave energy decreases faster than the WKB and reveal the presence of parametric interactions

Parallel temperature increases due to the generation of a velocity beam

Protons are perpendicularly heated by waves

Evolution of the proton distribution function

Wave-particle interactions provide signatures in the proton distribution function



Perpendicular heating due to ion-cyclotron interactions
Parallel acceleration due to non-linear interactions with parametric instability

Generation and evolution of a proton beam



Matteini et al. SSR 2011

Evolution of proton distribution and ion-beam anisotropic heating



The kinetic energy of the beam drift is converted in anisotropic proton heating through ion-beam instability (*Schwartz et al. 1981, Daughton and Gary, 1998*)

Evolution in the parameter space

The presence of a cyclotron perpendicular heating changes the trajectory of the system in the parameter space with respect the adiabatic case.



Cyclotron heating in the presence of minor ions (*Hellinger et al. 2005, Matteini et al. 2011*)



Power absorbed by different species through frequency sweeping Perpendicular preferential heating of minor ions

Oblique propagation: Parametric Decay 1-D



Enhancement of density fluctuations

Growth of an ionacoustic mode

Damping of the mother wave

Generation of a backward propagating daughter Alfvén wave

Oblique propagation: Parametric Decay 1-D



Growth rate at different angles

The instability growth rate decreases with increasing θ_{kB}

Table 1. Growth rate of parametric decay at various angles. For each angle we report the measured growth rate γ and the corresponding $\gamma_{\parallel} = \gamma/\cos(\theta)$

Run	θ_{kB}	k_0	k_s	k_{-}	γ	γ_{\parallel}
Α	30	0.21	0.33	0.12	0.15	0.17
В	45	0.21	0.33	0.12	0.12	0.17
\mathbf{C}	60	0.21	0.33	0.12	0.08	0.16

Evolution of proton distribution

Non-linear trapping by ion-acoustic waves generates velocity beams, like in the case of parallel mother waves (*Matteini et al., JGR 2010*)



Oblique Decay 2-D



Any role of transverse couplings?

Perpendicular couplings and transverse modulation of B



Perpendicular couplings and transverse modulation of B



Perpendicular couplings and transverse modulation of B



3-wave resonance along B

$$k_{\parallel}^{-}=k_{0\parallel}-k_{s\parallel},$$

$$k_{\perp}^{-}=k_{0\perp}-k_{s\perp}.$$

no constraint across B

Resonant condition satisfied also for frequencies (phase velocity depends only on k_{\parallel})



 $\mathbf{B}_{\mathbf{Z}}$

density

Evolution of fields

linear phase

post-saturation



Main modulation occurs across the magnetic field B_0

Conclusions

• Adiabatic evolution (i.e., absence of interactions and dissipation) does NOT mean to keep Maxwellian distributions and can also be quite complicated.

• Anisotropy of distribution functions is an important aspect that has to be taken into account. Plasma instabilities driven by temperature anisotropies or secondary beams play a role in the solar wind thermodynamics and possibly influence turbulence, reconnection, and cosmic rays acceleration.

• Data suggest the presence of a proton perpendicular heating in the solar wind, while a parallel cooling (or beam deceleration) is observed along the magnetic field. Constraints on heating models!

 Wave-wave interactions driven by parametric instabilities also contribute to the proton evolution with the generation of a velocity beam.
 The presence of oblique mother waves leads to broadband couplings for the daughter waves and large oblique spectra, with strong modulation across the mean magnetic field.

magnetic field

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