Geometric and Asymptotic Group Theory II

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Blatt 6 Amenability

- (1) Show that if $F \emptyset l_S G = 0$ wrt some finite generating set S, then $F \emptyset l_{\widetilde{S}} G = 0$ wrt any other finite generating set \widetilde{S} of G.
- (2) Show that if $F \emptyset l_S G = 0$ wrt one of the definitions of the boundary, then $F \emptyset l_S G = 0$ wrt any other boundary.
- (3) Show that the direct product of two amenable groups is itself amenable.
- (4) Is the Baumslag-Solitar group $BS(2,3)=\langle a,t\mid ta^2t^{-1}a^{-3}\rangle$ amenable? What is its growth?
- (5) Prove that the Baumslag-Solitar group $BS(1,2)=\langle a,t\mid tat^{-1}a^{-2}\rangle$ is amenable. What is its growth?