Problem Set 4 Due Friday, May 4.

Real Analysis

Math 131A, Spring Quarter 2018

- 1. Do problems 9.1 (b), 9.4, 9.9, 9.10, 9.11, 9.15, 10.7, 10.10 in the textbook.
- 2. Suppose (s_n) , (t_n) are sequences of real numbers such that for each $\varepsilon > 0$, there is n_0 such that for all $n \ge n_0$ we have $|s_n t_n| < \varepsilon$. Let $s \in \mathbb{R}$ such that $s_n \to s$. Prove that also $t_n \to s$.
- 3. (Extra credit.) Consider the sequence (e_n) given by $e_n = \left(1 + \frac{1}{n}\right)^n$ for each $n \ge 1$. Show that $e_n \le 3$ for each $n \ge 1$.